Circle True or False or leave blank. (1 point for correct answer, -1 for incorrect answer, 0 if left blank)

- 1. True False It is possible for a BVP to have exactly 2 solutions.
- 2. True False If y_1, y_2 are two solutions to a linear homogeneous differential equation, then $y_1 + y_2$ is.

Show your work and justify your answers. Please circle or box your final answer.

3. (10 points) (a) (5 points) Find the general solution to y'' + 2y' + 2y = 0.

(b) (4 points) Give an IVP involving a second order differential equation such that $y(t) = e^{2t} - e^t$ is a solution.

(c) (1 point) Prove that
$$\tan(\theta) = \frac{1}{i} \cdot \frac{e^{i\theta} - e^{-i\theta}}{e^{i\theta} + e^{-i\theta}}.$$